

Evaluate using a calculator. Round to three decimal places.

1. $\ln 24$ 3.178

Simplify each expression.

2. $3^{\ln 3}$

3

3. $5 \ln 7$

$$5 \cdot 7 = \boxed{35}$$

Expand each expression.

4. $\ln \frac{7x^3}{y}$

exponents at the end

$$\ln 7x^3 - \ln y$$

$$\ln 7 + \ln x^3 - \ln y$$

$\ln 7 + 3 \ln x - \ln y$

Condense each expression.

5. $2 \ln 8 + \frac{1}{2} \ln a - 4 \ln b$

exponents first!

$$\ln 8^2 + \ln a^{1/2} - \ln b^4$$

$$\ln 64 \sqrt{a} - \ln b^4 = \boxed{\ln \frac{64 \sqrt{a}}{b^4}}$$

Solve each equation using the natural logarithm function.

6. $7^x = 18$

$$\ln 7^x = \ln 18$$

$$\frac{x \ln 7}{\ln 7} = \frac{\ln 18}{\ln 7}$$

$$x = \frac{\ln 18}{\ln 7} \approx \boxed{1.485}$$

Solve each equation.

$$7. \quad 25 \ln x = 225$$
$$\div 25 \quad \div 25$$

$$\ln x = 9$$

$$e^{\ln x} = e^9$$

$$x = e^9 \approx 8103.084$$

$$8. \quad \ln(x+4) = 10$$

$$e^{\ln(x+4)} = e^{10}$$

$$x+4 = e^{10}$$
$$-4 \quad -4$$

$$x = e^{10} - 4$$

$$\approx 22022.466$$

Use the formula $N(t) = N_0 e^{-0.00012t}$ to solve.

9. A fossil is found that contains 35% of its original amount of carbon-14. How old is the fossil?

$$N(t) = N_0 e^{-0.00012t}$$

$$\frac{0.35 N_0}{N_0} = \frac{N_0 e^{-0.00012t}}{N_0}$$

$$0.35 = e^{-0.00012t}$$

$$\ln 0.35 = \ln e^{-0.00012t}$$

$$\frac{\ln 0.35}{-0.00012} = \frac{-0.00012t}{-0.00012}$$

$$t = \frac{\ln 0.35}{-0.00012}$$

$$\approx 8748.5$$

$$t \approx 8749 \text{ yrs old}$$