


4.2 Order of Operations

Mathematics agree to follow a set of rules so there is only one correct answer when you simplify an expression. Use the order of operations when you simplify an expression.

1. First perform operations within grouping symbols. (Parentheses, brackets, or fraction bars)
2. Next simplify numbers with exponents.
3. Then multiply or divide from left to right.
4. Finally add or subtract from left to right.

ORDER

always work LEFT \rightarrow RIGHT

PRACTICE:																																
$3 + 7 \times 6 \div 3 =$ $3 + 42 \div 3 =$ $3 + 14 =$ 17	$(6 \times 4) \div 3 - 6 + 2 =$ $24 \div 3 - 6 + 2 =$ $8 - 6 + 2 =$ $2 + 2 =$ 4	$2^2 \times 9 \div 3 =$ $4 \times 9 \div 3 =$ $36 \div 3 =$ 12																														
	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr><td style="text-align: center;">P</td><td style="text-align: center;">Please</td><td style="text-align: center;">Parentheses</td></tr> <tr><td style="text-align: center;">E</td><td style="text-align: center;">Excuse</td><td style="text-align: center;">Exponents</td></tr> <tr><td style="text-align: center;">M</td><td style="text-align: center;">My</td><td style="text-align: center;">Multiply</td></tr> <tr><td style="text-align: center;">D</td><td style="text-align: center;">Dear</td><td style="text-align: center;">Divide</td></tr> <tr><td style="text-align: center;">A</td><td style="text-align: center;">Aunt</td><td style="text-align: center;">Addition</td></tr> <tr><td style="text-align: center;">S</td><td style="text-align: center;">Sally</td><td style="text-align: center;">Subtraction</td></tr> </table>	P	Please	Parentheses	E	Excuse	Exponents	M	My	Multiply	D	Dear	Divide	A	Aunt	Addition	S	Sally	Subtraction	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: center; vertical-align: middle;">P</td> <td style="text-align: center; vertical-align: middle;">Parentheses $()$</td> </tr> <tr> <td style="text-align: center; vertical-align: middle;">E</td> <td style="text-align: center; vertical-align: middle;">Exponents x^5</td> </tr> <tr> <td style="text-align: center; vertical-align: middle;">M</td> <td style="text-align: center; vertical-align: middle;">Multiply \times</td> </tr> <tr> <td style="text-align: center; vertical-align: middle;">D</td> <td style="text-align: center; vertical-align: middle;">Divide \div</td> </tr> <tr> <td style="text-align: center; vertical-align: middle;">A</td> <td style="text-align: center; vertical-align: middle;">Addition $+$</td> </tr> <tr> <td style="text-align: center; vertical-align: middle;">S</td> <td style="text-align: center; vertical-align: middle;">Subtraction $-$</td> </tr> </table>	P	Parentheses $()$	E	Exponents x^5	M	Multiply \times	D	Divide \div	A	Addition $+$	S	Subtraction $-$
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$$\begin{aligned}
 & 3 \times (3 + 7) - 4^2 \div 2 \\
 & = 3 \times 10 - 4^2 \div 2 \\
 & = 3 \times 10 - 16 \div 2 \\
 & = 30 - 8 \\
 & = 22
 \end{aligned}$$

$$\begin{aligned}
 2 \times 4^2 + 5^2 \div (26 - 1) &= 2 \times 4^2 + 5^2 \div (26 - 1) \\
 &= 2 \times 4^2 + 5^2 \div (25) \\
 &= 2 \times 4^2 + 5^2 \div 25 \\
 &= 2 \times 16 + 25 \div 25 \\
 &= 2 \times 16 + 1 \\
 &= 32 + 1 \\
 &= 33
 \end{aligned}$$

Example: Use the order of operations to simplify. $\frac{1.3}{3.3}$

1.) $18 \div 3 + 4$

$$\begin{aligned}
 & 6 + 4 \\
 & \textcircled{10}
 \end{aligned}$$

$$\begin{array}{r}
 11 \\
 \times 33 \\
 \hline
 33 \\
 330 \\
 \hline
 363
 \end{array}$$

$$\begin{array}{r}
 38.0 \\
 + 36.3 \\
 \hline
 74.3
 \end{array}$$

2.) $5 + (36 - 3) + 11 \times [1.3 + 2.0]$

$$5 + (36 - 3) + 11 \times 3.3$$

$$5 + 33 + 11 \times 3.3$$

$$5 + 33 + 36.3$$

$$38.0 + 36.3$$

$$\boxed{74.3}$$

Example: Use the order of operations to simplify.

3.) $(50 \div 25)^2 \times 2 + 5 \times 0.3$

$2^2 \times 2 + 5 \times 0.3$

$4 \times 2 + 5 \times 0.3$

$8 + 5 \times 0.3$

$8 + 1.5$

9.5

$\begin{array}{r} 5 \\ \times 3 \\ \hline 15 \end{array}$

$\begin{array}{r} 8.0 \\ + 1.5 \\ \hline 9.5 \end{array}$

4.) $2^2 \times (15 - 3)$

$2^2 \times 12$

4×12

48

Example: Insert parentheses as needed to make each equation true.

5.) $14 + 6.6 \div (0.2 + 0.4) = 25$

$14 + 6.6 \div 0.6$

$14 + 11$

25

$\begin{array}{r} 6.6 \\ 6 \overline{) 6.6} \\ \underline{-6.6} \\ 0 \end{array}$

6.) $5 \times 10^2 \div (41 - 4^2) = 20$

$5 \times 10^2 \div (41 - 16)$

$5 \times 10^2 \div 25$

$5 \times 100 \div 25$

$500 \div 25$

20